IMAGING BY SEISMIC INVERSION BASED ON THE ADJOINT STATE METHOD

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Summary

Least-squares migration (LSM) has the ability to compensate for limitations in the imaging system and estimate an image that is closer to the earth reflectivity. These favourable properties over conventional imaging have made it the method of choice in complex geological settings.

In this paper, we discuss the different properties of LSM and Full Waveform Inversion (FWI) and suggest a new nonlinear least-squares reverse time migration (LS-RTM) implemented in the framework of FWI. The new inversion solution iteratively estimates the earth reflectivity while simultaneously updating the velocity model. We demonstrate the effectiveness of the method through a case study from the Norwegian Sea.

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Introduction

LSM is a linear inversion process with a convex objective function. It updates the reflectivity by matching the high wavenumber perturbations in the observed and synthetic data (Nemeth et al., 1999). The linear property of the inversion relates to the fixed background model, meaning that the velocity field is assumed known and kept unchanged during the inversion, making it feasible to estimate with a linear solver (Gauthier et al 1986; Mora 1989). The synthetic data are generated based on the Born approximation, where only the first order scattering term is utilized in the forward modeling step (Woodhouse 1980; Tanimoto 1984). In practice, this means that only the near- to mid-reflection angles can be utilized in the inversion process.

On the other hand, FWI is a highly nonlinear inversion with a complex objective function consisting of many local minima (Tarantola 1987). The aim of FWI is to minimize the misfit between observed and modeled data. To linearize this nonlinear inversion, the model parameters can be updated with a gradient descent approach that utilizes small steps/learning rate in combination with a multi-stage process. In practice, this means that the lowest frequencies are first utilized and matched before higher frequencies are included in the inversion, to reveal more details in the model. FWI is commonly implemented with the adjoint-state-method (Chavent 1974), where the adjoint states refer to the backpropagated data-residuals and the gradient of the least-squares misfit is a migration operator (Lailly 1983; Tarantola 1984). Refractions and diving waves have proven to be robust and easy to utilize in FWI and have become default in most velocity model building projects. FWI can as well incorporate reflections, which allow velocity estimation beyond the penetration depth of diving waves. For this to be feasible, the modeling engine will have to initiate the complete wavefield; diving waves, refractions and reflections (beyond Born approximations).

We therefore propose a new nonlinear seismic inversion process, based on the FWI framework, that utilizes the full acoustic wavefield, not limited by Born modeling. The method can be considered as a multi-parameter FWI, where each model will be updated simultaneously without parameter-leakage. This can be achieved with a unique imaging condition, that naturally honours the seismic scale separation, and solve for the background model (velocities) and the perturbations (reflectivity) separately. The background model can be interpreted as the FWI velocities and the reflectivity can be described as a nonlinear LS-RTM, implemented with the adjoint state method. To handle the nonlinearity of this inversion, we follow the multi-stage approach until the background model reach convergence. From this point, we can perform large steps in frequency with the focus on the reflectivity model alone.

The new implementation has been tested on a dataset over the recent 'Slagugle discovery' in PL-891, located 14 miles from the Heidrun field in the Norwegian Sea. The water depth is between 300-400 meters and the geology is characterized by heavily rotated fault blocks with large lateral velocity variations.

Methodology

Different implementations of LSM exist in both the image and data space, with curvelet domain matching filters, Point Spread Functions (PSFs) and the full iterative LSM (Guitton, 2004; Valenciano, 2008; Lu et al., 2017). Existing solutions include both ray-based and wave-theoretic migrations (Korsmo et al., 2019, 2021). A fundamental requirement is that the velocity model is assumed to be known and unchanged during the inversion. Errors in the velocity model may lead to instability issues and noisy results for the data-domain approach (Wang et al., 2021), as well as sub-optimal amplitude corrections with the image-domain implementation. To mitigate the kinematic misalignments due to an imperfect velocity model, a warping step prior or during the data-domain LSM, can be a pragmatic solution to stabilize the inversion (Luo et al., 2014). This approach will not focus the energy at the correct location in the sub-surface since the observed data gets shifted to the modeled data. A desired solution would be

to refine the velocity model while inverting for the reflectivity. To achieve this, a natural approach would be to take a closer look at FWI, since RTM and FWI share the same modeling/migration engine and sensitivity kernels. The RTM/FWI sensitivity kernel consists of three different components; the "banana" related the diving waves, the "rabbit ears" generated by reflections, and the migration isochrones. The first two, contribute to the tomography kernel while the latter can be described as the impedance or reflectivity kernel.

Recent work has shown that FWI, with the access to modern compute resources, can be extended to high frequencies. The final high-resolution velocity model can post-inversion be converted to pseudo-reflectivity through a simple derivation step (Zhang et al., 2020; Kalinicheva et al., 2021). This approach will essentially leak reflectivity into the velocity model when implemented using a conventional cross-correlation imaging condition. Even when a density model is employed, it only acts as a passive parameter during FWI and all reflectivity changes are simply mapped as velocity updates.

To reduce this parameter leakage, we make use of an alternative approach to keep the background model and the reflectivity separated and update them simultaneously during the inversion process (Yang et al., 2021). This can be achieved by separating the tomography from the reflectivity kernel using Inverse Scattering Imaging Condition during the inversion process (Whitmore and Crawley 2012; Ramos-Martinez et al., 2016). The process will isolate the tomographic kernel from the reflectivity kernel and use it to update the background model, which controls the kinematics and structural imaging. On the other hand, the reflectivity kernel will only contain the migration isochrones, and will be used to update the LS-RTM by matching the amplitudes between observed and modeled data. In order to utilize the full acoustic wavefield to update the velocity model, our solution utilizes an alternative formulation of the wave-equation, based on vector reflectivity modeling, to simulate all acoustic wave modes observed in the data (Whitmore et al., 2020).

Field data examples

The new nonlinear data-domain LS-RTM was tested on a field data example from the Norwegian Sea over the 'Slagugle discovery'. We used a vintage velocity model and a fully pre-processed data for the test. The inversion however can also be performed using raw data that includes free-surface multiples. By setting proper boundary conditions, the forward modeling engine can generate synthetic data that is consistent with the input field data for either scenario. When using raw data, the multiples crosstalk generated by the imaging of multiples can, in principle, be attenuated by the iterative inversion process (Lu et. al 2018).

In figure 1a-b, we show the 25Hz frequency comparison of initial (RTM) and updated nonlinear LS-RTM. The corresponding FK-spectra and amplitude spectrum are shown in figure 1c-e, where the nonlinear LS-RTM clearly broadens the wavenumber content both laterally and vertically. The inverted reflectivity shows a much-improved image, with a balanced amplitude response, enhanced resolution, and improved fault imaging.

Jointly with the reflectivity updates, a refinement of the velocity model was achieved. Figure 2a shows the accumulated velocity perturbation and 2b shows the angle gathers from one-way wave-equation migration. The flatness of the angle gathers from the refined velocity model indicate a well resolved background model. Notice that the velocity perturbations are structurally consistent, and the updates penetrate to the full image range (where there is reflectivity in the image). This was made possible by utilizing the full seismic wavefield in the inversion process, including reflections.

Figure 3 shows the data-domain QC for a single shot gather in the middle of the cross-section. The observed data is shown in 3a, the modeled data with initial model compared to the updated one are in 3b-c and the corresponding data-residuals in 3d-e. The updated reflectivity and velocity clearly improve the data-match and result in reduced data-residuals as annotated by the arrows.
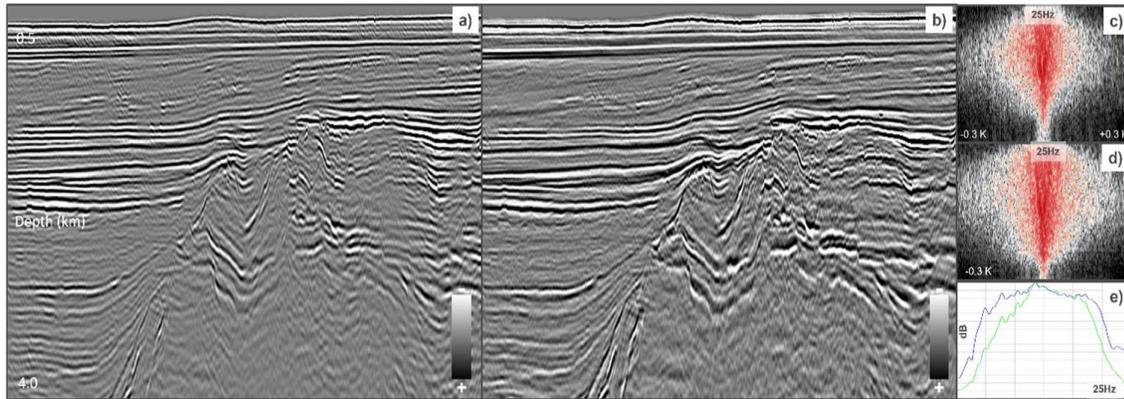
Figure 1 *Comparison of RTM (a) and the new data-domain LS-RTM (b) with the corresponding FK-spectra in (c) and (d). Comparison of the amplitude spectra are shown in (f), where the green cure corresponds to RTM and the blue curve shows the LS-RTM. Notice the improvements in the wavenumber content, amplitude fidelity, structural imaging and fault mapping in the LSRTM results compared to the RTM.*
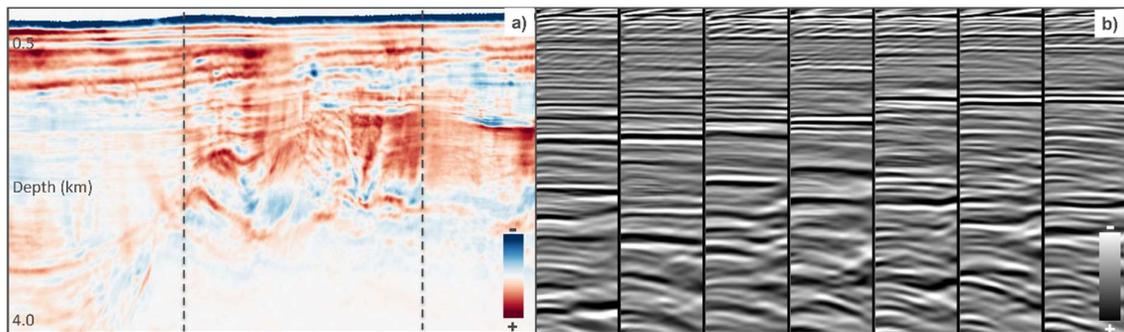
Figure 2 *Accumulated velocity difference with +/- 100m/s display range (a) and imaging QC of the refined velocity model through the centre of the line, between the two stipulated lines (b). The velocity updates are structurally consistent with the image and produce flat angle gathers computed with wave-equation migration.*

Conclusions

We have demonstrated how our new nonlinear data-domain LS-RTM, implemented using the adjoint state method, can invert for the reflectivity while simultaneously refining the FWI velocity model. This mitigates the need to stabilize the data-domain LSM with a warping process. The implementation takes advantage of the similarities between RTM and FWI and our unique imaging condition to carefully update the velocity and reflectivity without any leakage between the two models. In particular, reflectivity changes caused by density variations are not erroneously mapped as velocity updates. The inversion utilizes the full acoustic wavefield through an alternative formulation of the wave-equation parametrized in terms of velocity and vector reflectivity. The nonlinear LS-RTM results show significant structural improvements, more focusing, and better fault imaging compared to the RTM.

Acknowledgements

We thank PGS for the permission to present this work.
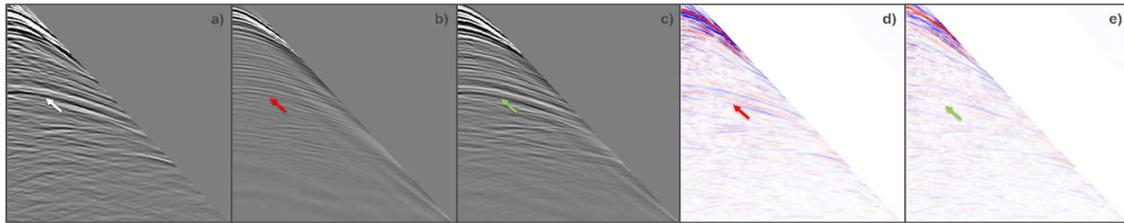
Figure 3 *Recorded shot gather after full pre-processing (a), synthetic data with the initial reflectivity/velocity models (b) and with updated models (c) and the corresponding initial (d) and updated data-residuals (e). Notice the improved data-match after inversion and the reduction in the data-residuals after inversion, as annotated by the arrows.*

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